

Thermal Assessment of Naturally Cooled Electronic Enclosures With Rectangular Fins

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Passive heat transfer from enclosures with rectangular fins is studied both experimentally and theoretically. Several sample enclosures with various lengths are prepared and tested. To calibrate the thermal measurements and the analyses, enclosures without fins ("bare" enclosures) are also prepared and tested. Surface temperature distribution is determined for various enclosure lengths and heat generation rates. Existing relationships for natural convection and radiation heat transfer are used to calculate the heat transfer rate from the tested samples. The theoretical results successfully predict the trends observed in the experimental data. It is observed that the contribution of the radiation heat transfer is on the order of 50% of the total heat transfer for the tested enclosures. As such, a new correlation is reported for calculating an optimum fin spacing for vertically-mounted uniformly finned surfaces, with rectangular straight fins that takes into account both natural convection and radiation. [DOI: 10.1115/1.4007077]

Keywords: electronic enclosures, conjugate heat transfer, fin spacing, natural convection

1 Introduction

Passive cooling, technologies or design features without power consumption, has been used in thermal solutions for various applications such as power electronics, telecommunications, microelectronics, as well as heating, ventilation, and air conditioning (HVAC) systems. Two significant heat transfer modes involved in passive cooling systems are natural convection and radiation. Convection heat transfer from an object, determined using Newton's cooling law ($Q_{\text{conv}} = hA(T_s - T_\infty)$), can be enhanced by increasing the heat transfer coefficient, h , and/or by increasing the surface area, A , if the temperature difference is fixed [1].

Extended surfaces, which are popularly known as fins, are extensively used in air-cooled heat exchangers and electronic cooling. Although fins increase the surface area, they lead to an increase in frictional resistance resulting in a lower air flow rate in the vicinity of the finned surface. At the same time, they add more thermal resistance to the conduction path from the base to the ambient. As such, the heat transfer coefficient for noninterrupted finned surfaces is lower than the value for the base plate without

fins. Therefore, the overall heat transfer rate of a finned plate could either increase or decrease in comparison with the base plate without fins. These competing trends clearly indicate the need for an optimization study to establish an 'optimum' fin design for air cooled enclosures. The effect of fin-spacing on natural convection has been investigated by several researchers. Design information of natural convection for fin arrays can be extracted from experimental studies of Starnner and McManus [2], Welling and Wooldridge [3], Harahap and McManus [4], Jones and Smith [5], Donovan and Roher [6], Van de Pol and Tierney [7], Yuncu and Anbar [8], and Guvenc and Yuncu [9], as well as the theoretical works of Bar-Cohen and Rohsenow [10], Baskaya et al. [11], Haddad and Bany-Youness [12], and Dialameh et al. [13]. As a result, several correlations have been reported for the optimum fin spacing and the natural convection from heat transfer rate as a function of geometrical parameters.

Radiation heat transfer from a surface located in an ambient of temperature T_∞ can be calculated from [1]:

$$Q_{\text{rad}} = \frac{F_{s\infty} A \epsilon \sigma (T_s^4 - T_\infty^4)}{F_{s\infty} (1 - \epsilon) + \epsilon} \quad (1)$$

where $F_{s\infty}$ is the surface view factor, ϵ is the surface emissivity coefficient, and σ is the Stefan-Boltzman constant $5.67 \times 10^{-8} \text{ W/m}^2\text{K}^4$. Although fins increase the surface area, they can block part of radiation from the base plate and adjacent fins which reduces the surface view factor in Eq. (1). As such, similar to natural convection, radiation heat transfer also depends on the spacing and other geometrical parameters of the finned surface.

Radiation heat transfer plays an important role in heat transfer from fin arrays. This has been shown by Edwards and Chaddock [14], Chaddock [15], Sparrow and Acharya [16], Saikhedkar and Sukhatme [17], Sparrow and Vemuri [18,19], Azarkish et al. [20], and Rao et al. [21]. It has been reported that the radiation heat transfer contributes between 25–40% of the total heat transfer from fin arrays.

The listed studies have been focused on heat transfer from one single finned plate. Cha and Cha [22,23] investigated laminar steady gravity-driven flow around a single isothermal cube in an infinite medium by employing a control volume finite difference technique. Natural convection from isothermal cuboids and other geometries has been studied by Radziemska and Lewandowski [24,25] and Jafarpour and Yovanovich [26] both experimentally and numerically.

In spite of numerous existing studies on natural convection, our literature survey reveals a lack of experimental and theoretical studies on finned enclosures with conjugate natural convection and radiation heat transfer. To cover this ground, passive conjugate heat transfer from enclosures with rectangular shaped fins has been investigated theoretically and experimentally in this study. A custom-designed testbed has been built to perform the experiments. Several existing finned enclosures, currently being used by our industrial partner Analytic System Ware (Delta, BC, Canada) have been prepared and tested to assess their thermal performance. The test bed allows temperature and input power measurements needed to assess the steady-state heat transfer from the enclosures. Existing correlations in the literature are used to predict the overall heat transfer coefficient and the average temperature of the enclosures under natural convection and radiation heat transfer. The experimental data were in reasonable agreement with the theoretical results. The theoretical analysis is then used to draw conclusions on the effect of fin spacing on the overall heat transfer rate of the systems with conjugate heat transfer.

2 Experimental Approach

2.1 Tested Samples. Six electronic enclosures were prepared and tested in this study; the electronic enclosures were made of aluminum by extrusion process. Three enclosures were finned while the others had the fins milled off down to the level of the bottom of the fin, see Figs. 1 and 2 for more details. During the milling process, no alterations were made that affected the enclosures' length.

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Contributed by the Electronic and Photonic Packaging Division of ASME for publication in the JOURNAL OF ELECTRONIC PACKAGING. Manuscript received January 16, 2012; final manuscript received June 11, 2012; published online July 24, 2012. Assoc. Editor: Amy Fleischer.

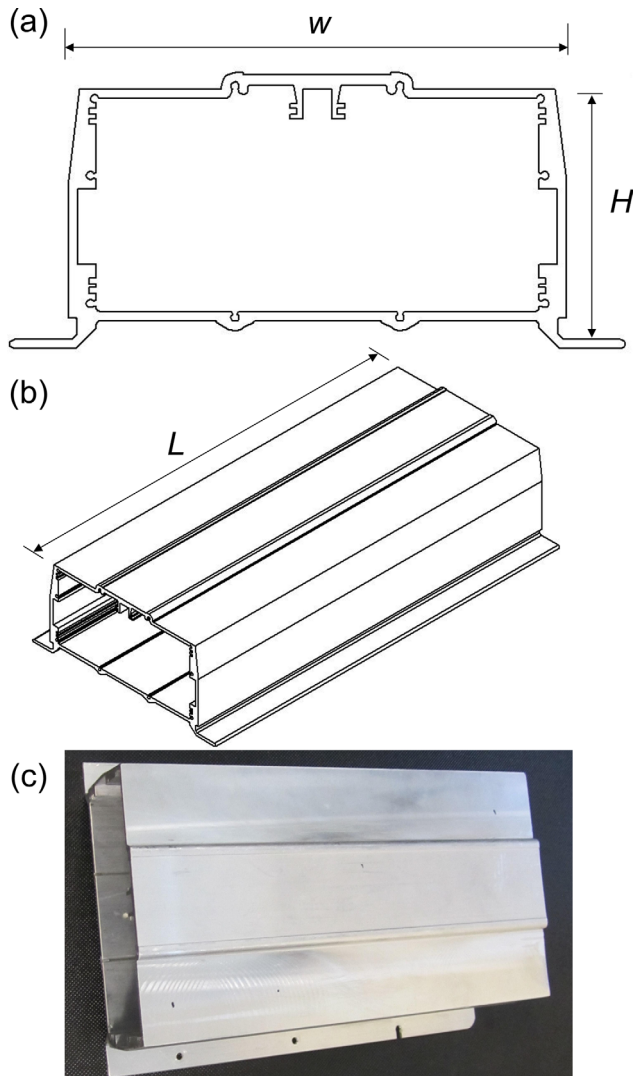


Fig. 1 Schematic of the finned enclosures: (a) cross-section view, (b) isometric view, and (c) an actual enclosure

The studied enclosures were used by our industrial partner. The enclosures' lengths were 25.40, 30.05, and 40.08 cm.

The enclosures' surface was not uniformly finned; as it can be seen in Fig. 1, they are comprised of unfinned (bare) surfaces and regions with uniformly distributed fins (with 2.5 mm spacing). The width of the bare regions is large enough, larger than 30 mm, such that the surface can be modeled as bare plate. The dimensions of the tested enclosures are listed in Table 1.

2.2 Experimental Procedure. Figure 3 shows the schematic and the actual testbed. A wooden board was used to mount the enclosures vertically. The only possible mechanism for unwanted heat transfer was through conduction to the back wall. The gap between the wooden board and the enclosure surface was filled

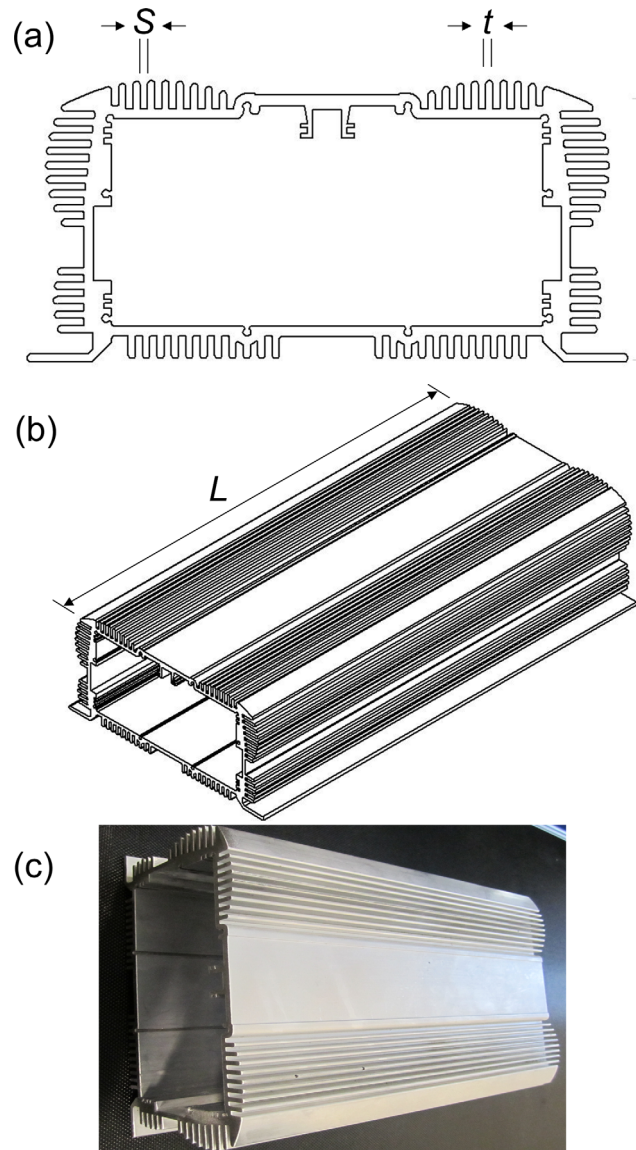


Fig. 2 Schematic of the bare enclosures without fins: (a) cross-section view, (b) isometric view, and (c) an actual enclosure

with a thick layer of foam for thermal insulation. It was assumed that the conductive heat transfer through the wooden board was negligible in comparison with the radiation and convection heat transfer from the enclosure to the ambient.

Enclosure ends were capped with 8 mm thick Poly(methyl methacrylate) (PMMA) plates to provide an airtight seal to the inside, as well as to limit heat transfer from the end regions. End caps were cut to match the profile of the extrusion so as not to disturb the gravity-driven airflow.

Chromalox strip heaters of 20 cm length were purchased from Omega (Toronto, ON) and were installed inside the enclosures to

Table 1 Dimensions of the tested enclosures

Enclosure name	Enclosure type	Length (m)/(in)	Fin spacing (m)	Finned area (m ²)	Bare area (m ²)
B10	Bare	0.254/10	0.0	0.0	0.085
B12	Bare	0.305/12	0.0	0.0	0.102
B16	Bare	0.408/16	0.0	0.0	0.137
F10	Finned	0.254/10	0.0025	0.079	0.078
F12	Finned	0.308/12	0.0025	0.095	0.094
F16	Finned	0.408/16	0.0025	0.127	0.126

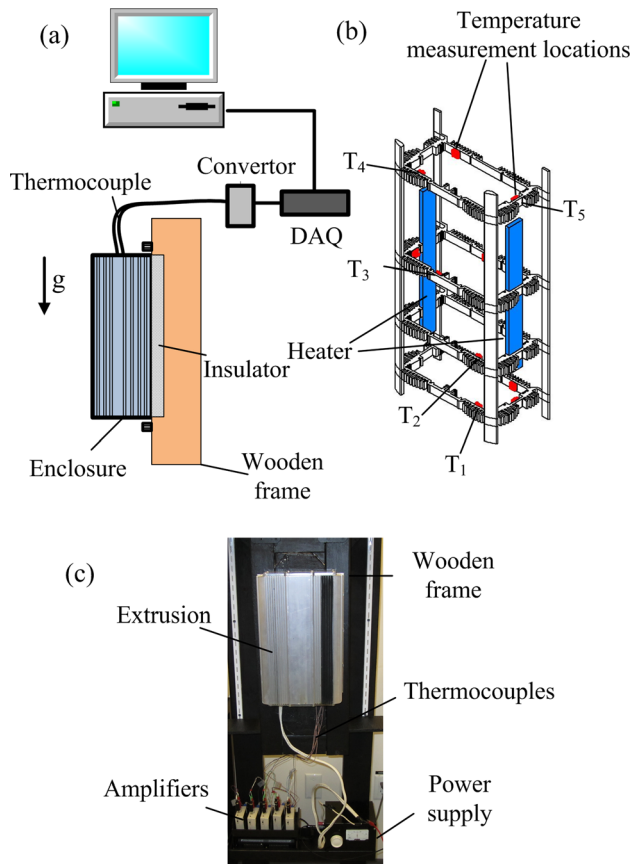


Fig. 3 Experimental test bed; (a) schematic, (b) distribution of temperature measuring points and the location of the heater inside the enclosures, (c) actual test bed

simulate heat generation from MOSFETs. Maximum rated power of each heater was 150 W. The heaters were powered by an adjustable AC power supply and the consumed power was monitored during the experiments. Ten self-adhesive T-type copper-constantan thermocouples with uncertainty of $\pm 1^\circ\text{C}$ were installed in various positions on the surface of the enclosures, see Fig. 3(b). All thermocouples were adhered to the inside surface of the enclosure to prevent disturbing the outside buoyancy-driven air flow. An additional thermocouple was used to measure the ambient room temperature during the experiments. Each thermocouple is plugged into a TAC80B-T thermocouple to analog converter supplied by Omega (Toronto, ON).

The enclosures were tested in a windowless room free of air currents. The room temperature was kept constant at 20°C . Each enclosure was tested at various power levels ranging from 20 to 110 W. The heaters were turned on and the surface temperature was monitored until a steady state condition is reached, i.e., the power input was equal to the heat transfer from natural convection and radiation. Once the variation of the surface temperature was less than 0.1°C/h , temperatures of all thermocouple were recorded and used in the analysis.

Figure 4 shows the maximum and minimum surface temperatures for enclosure F10 at various input power (heat transfer rates). As expected, the thermocouple closest to the lower edge of the enclosure showed the minimum temperature, T_1 ; the enclosure temperature increased at higher elevations due to thermal boundary growth and the maximum temperature occurred on the top of the enclosure, T_5 .

3 Theoretical Calculations

3.1 Enclosures Without Fins. Our experimental measurements showed that the maximum temperature difference along the

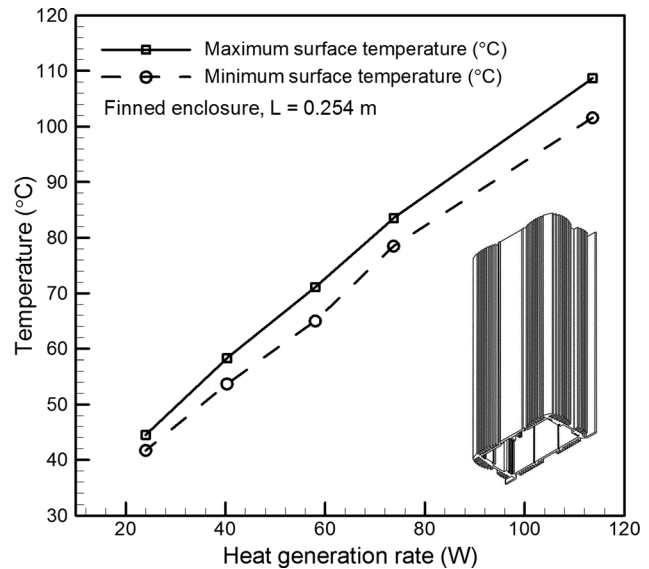


Fig. 4 The maximum and the minimum measured temperatures on the surface of the F10 enclosure

tested enclosures was less than 8°C . As an example, Fig. 4 shows the maximum and minimum surface temperatures for enclosure F10 at various input power (heat transfer rates). As such, the surfaces of the enclosure are assumed isothermal and the arithmetic average of the thermocouple readings is used in the analysis. The air properties are considered to be constant and are calculated at the film temperature as per the Nusselt number correlations used. The Nusselt number for natural convection from a plane vertical surface (bare enclosure) of length L can be calculated from the following equation [27]:

$$Nu = \frac{hL}{k} = \left\{ 0.825 + \frac{0.387Ra_L^{1/6}}{\left[1 + (0.492/Pr)^{9/16} \right]^{8/27}} \right\}^2 \quad (2)$$

where k is the thermal conductivity of air and Ra_L is the Rayleigh number based on the enclosures length:

$$Ra_L = \frac{g\beta(T_s - T_\infty)L^3}{\nu^2} Pr \quad (3)$$

where g is the gravity acceleration, β is coefficient of volume expansion, ν is kinematic viscosity of air, and Pr is Prandtl number. Nusselt number (and the heat transfer coefficient) is calculated from Eq. (2) and the natural convection heat transfer rate is calculated using Newton's cooling law [1]. The radiation heat transfer is calculated from Eq. (1) where the view factor $F_{s\infty}$ is assumed to be 1 in this study. Total heat transfer from an enclosure can be calculated from:

$$Q_{\text{total}} = Q_{\text{rad}} + Q_{\text{conv}} \quad (4)$$

Since with the exception of emissivity all other parameters for theoretical prediction of the heat transfer rate from bare surface are known, the experimental data can be used to estimate the emissivity. From comparison of the experimental data with the total heat transfer rate, one can estimate the surface emissivity coefficient to be $\varepsilon = 0.75$, for the tested enclosures. This value is in the range of the emissivity values (0.4–0.8) reported for aluminum alloys in heat transfer textbooks; see for example Ref. [1]. Therefore, $\varepsilon = 0.75$ is considered in all radiation heat transfer calculations including the finned enclosures.

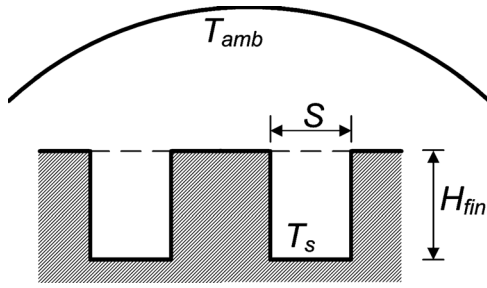


Fig. 5 The considered geometry for calculating $F_{s\infty}$

3.2 Finned Enclosures. For the finned enclosures shown in Fig. 1, the total area is divided into two regions: (i) unfinned region, and (ii) finned region. The heat transfer in the unfinned region is calculated similar to the approach described in Sec. 3.1. Due to a compact spacing and long fins of the tested enclosures, the air flow between the adjacent fins become fully-developed rather quickly; i.e., $L_{\text{fully-developed}}/L_{\text{enclosure}} < 0.01$. As a result, channel flow can be assumed, and the Nusselt number for the finned region can be calculated from [27]:

$$Nu_s = \frac{hS}{k} = \left\{ \frac{567}{(Ra_s S/L)^2} + \frac{2.873}{(Ra_s S/L)^{0.5}} \right\}^{-0.5} \quad (5)$$

where Ra_s is the Rayleigh number based on the fin spacing in the fin array, see Table 1. The radiation heat transfer is then calculated from Eq. (2) with $\varepsilon = 0.75$. $F_{s\infty}$ for the finned area (see Fig. 5) was calculated from:

$$F_{s\infty} = \frac{S}{H_{\text{fin}} \times 2 + S} \quad (6)$$

In the calculation, the average value of fin heights in Fig. 1 is used as H_{fin} .

4 Comparison of Experimental Data With Theoretical Calculations

The enclosures listed in Table 1 were tested with various heat generation rates under steady state condition as described in Sec. 2. For convenience, average surface temperatures are used in the present analysis. In Figs. 6 and 7, the experimental data for averaged surface temperature for the tested enclosures are plotted versus input power (heat generation) and compared with the theoretical predictions.

As can be seen from Figs. 6 and 7, the experimental data for the surface temperature can be successfully predicted by the present model, Eq. (5); the maximum relative difference between experimental and theoretical results is less than 9%. Also, the heat transfer enhancement from finned surfaces is minimal due to small fin spacing used in this particular enclosure design.

The contribution of both radiation and convection heat transfers in the total heat transfer rate from the unfinned (bare) and finned enclosures are plotted in Fig. 8. It can be seen that the radiation portion is larger than 50% for various surface temperatures. At lower surface temperatures the natural convection heat transfer is lower than the radiation counterpart. As the temperature increases, the contribution of the natural convection to the overall heat transfer rate increases. As a result of the nonlinear relationship between surface temperature and radiation heat transfer, in higher surface temperatures, the contribution of radiation to the overall heat transfer rate becomes more pronounced.

5 Optimum Fin Spacing

The maximum difference between the averaged surface temperature of the finned and bare enclosures tested, at the same heat

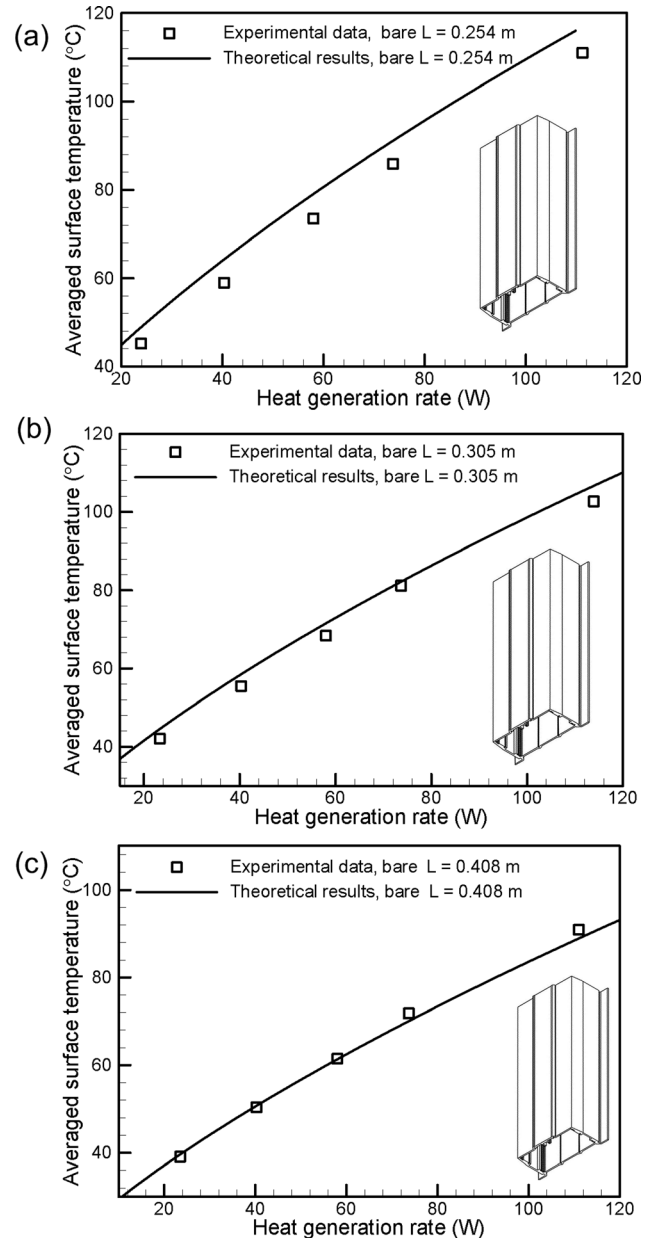


Fig. 6 Comparison of the experimental data with theoretical predictions for bare enclosures: (a) B10, (b) B12, and (c) B16

generation rate, was less than 4°C . The tested finned enclosures which were in use by our industrial partner had higher surface area by two folds and were 84% heavier than the bare one with the same length. In other words, fins did not contribute to heat transfer enhancement while adding to the manufacturing cost significantly. Therefore, use of the studied finned enclosures would not be economic unless the fins are properly designed.

According to Bar-Cohen and Rosenhow [10], a fin spacing in the range of 7–12 mm (depending on the enclosure surface temperature) should result in the maximum natural convection for the tested samples. However, the fin spacing in the tested samples is 2.5 mm, which is much smaller than the recommend spacing by Ref. [10]. As a result, the heat transfer coefficient is significantly lower than the one for a bare plate. Moreover, the compactness of the fins leads to smaller surface view factors in the finned region.

The theoretical model, Eqs. (1)–(6), which is verified through comparison with experimental data, is used to investigate effects

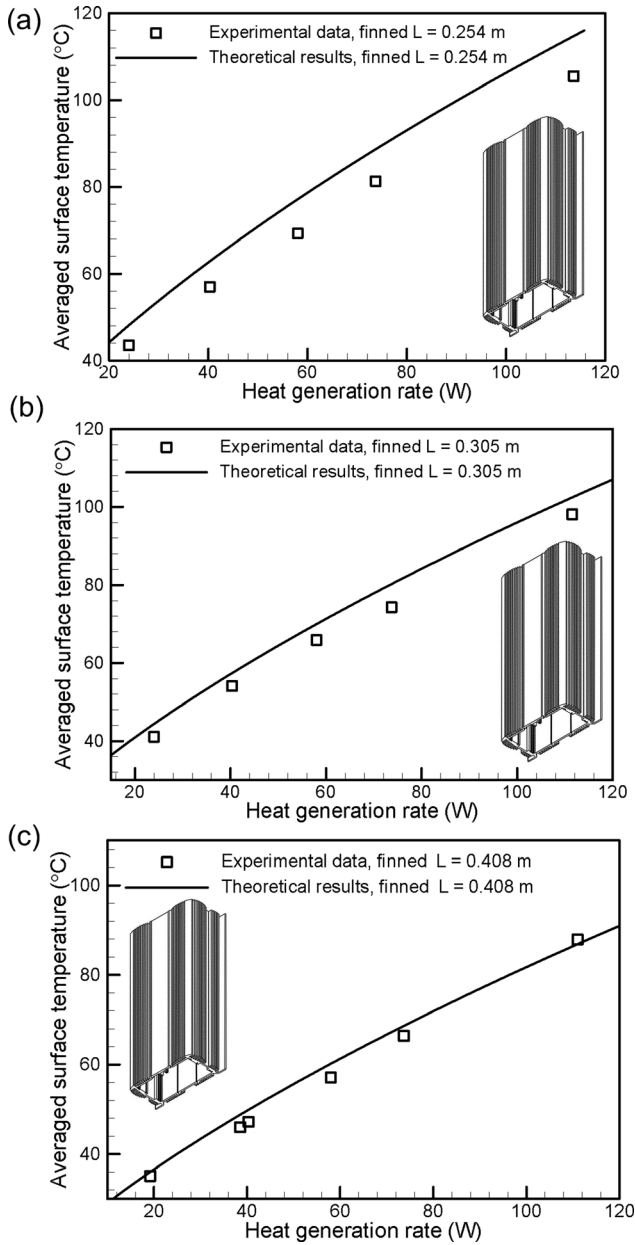


Fig. 7 Comparison of the experimental data with theoretical predictions for finned enclosures: (a) F10, (b) F12, and (c) F16

of fin spacing on the overall heat transfer rate from the finned enclosures uniformly finned. Figure 9 shows the calculated results for various surface temperatures. Moreover, the optimum fin spacing values, obtained from Fig. 9, are compared with the values proposed by Bar-Cohen and Rosenhow [10] in Table 2. The optimum fin spacing can be calculated from the following relationship:

$$S_{opt} = 0.0231 \times (T_s - T_\infty)^{-0.236} \quad (7)$$

The proposed new relationship in Eq. (7) is valid for a more general case where mixed convection and radiation heat transfer occur. It is noteworthy that the fins designed using Eq. (7) have a higher thermal performance (at least 10%) compared to those designed using the Bar-Cohen and Rosenhow correlation [10]; this is due to the importance of radiation heat transfer.

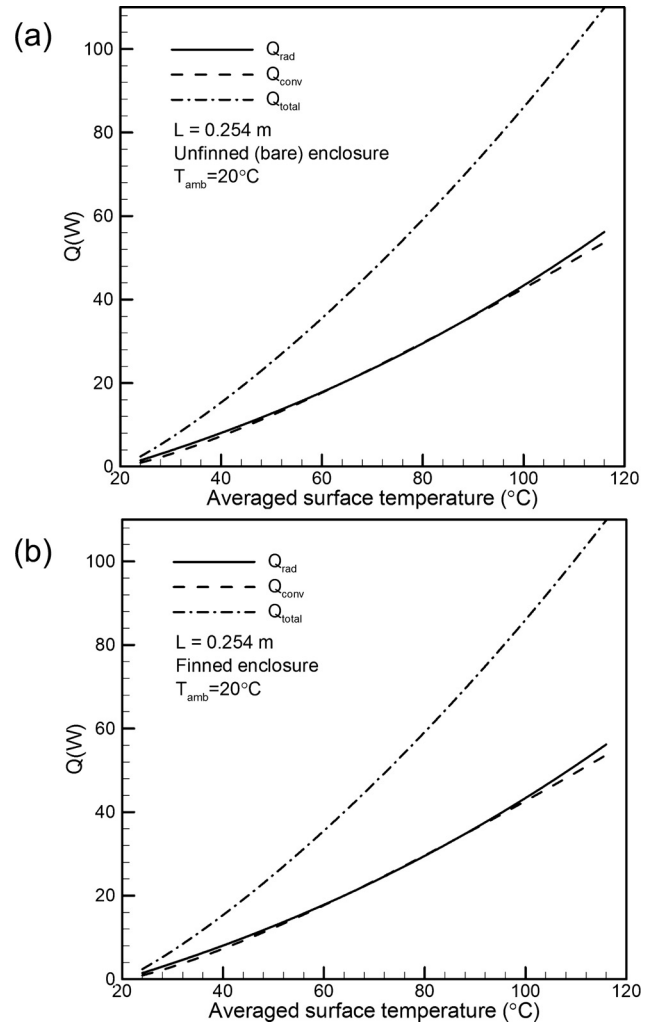


Fig. 8 Contribution of radiation in the overall heat transfer: (a) bare enclosures, (b) finned enclosures

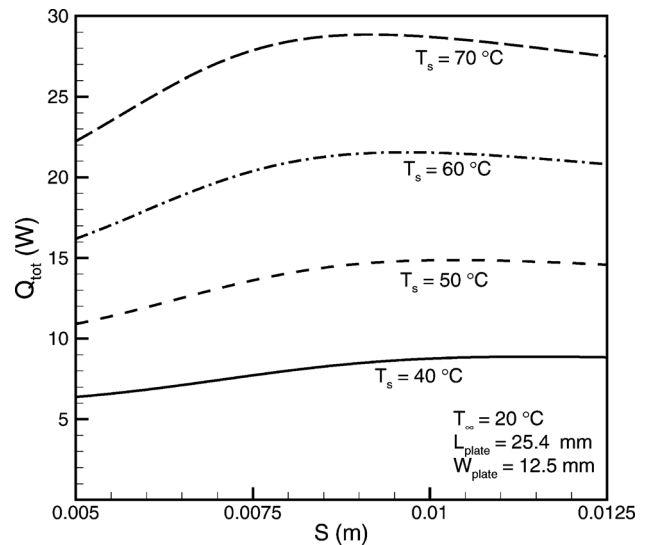


Fig. 9 Effect of fin spacing on conjugate heat transfer from a uniformly finned surface

Table 2 Optimum fin spacing for the maximum conjugate heat transfer from uniformly finned plates (the present study) and for natural convection from surfaces [10]

T_∞	T_s	S_{opt} present study, Eq. (7) (mm)	S_{opt} [10] (mm)
20	40	11.4	10.1
20	50	10.4	9.2
20	60	9.6	8.6
20	70	9.2	8.2

6 Conclusions

Heat transfer from 6 different finned and bare enclosures in-use by our industrial partner, Analytic System Ware (Delta, BC, Canada), was studied experimentally and analytically. The averaged surface temperature was measured for various heat generation rates. The arithmetic average surface temperature was also calculated using existing relationships for natural convection and radiation heat transfer. The theoretical results were in good agreement with the experimental data. Our analysis showed that more than 50% of the overall heat transfer from the tested samples was due to radiation. Moreover, the fin spacing had a significant impact on the cooling capacity. Due to small fin spacing in the tested samples, existing fin design did not improve the surface temperature while increasing the production costs and enclosure weight by 84%. In addition, a new compact relationship was reported for optimum fin spacing for the maximum conjugate heat transfer from a uniformly finned enclosure under various surface temperatures.

Acknowledgment

Financial support of Natural Science and Engineering Research Council (NSERC) of Canada is gratefully acknowledged. Authors thank our industrial partner, Analytic Systems Ware Ltd. (Delta, BC, Canada), for their technical support and financial assistance.

Nomenclature

A	= surface area, m^2
F_{∞}	= view factor
g	= gravitational acceleration, m^2/s
h	= heat transfer coefficient, W/m^2K
H	= enclosure height, m
k	= thermal conductivity, W/mK
L	= enclosure length, m
Nu	= Nusselt number
Pr	= Prandtl number
Q	= heat transfer rate, W
Ra	= Rayleigh number
S	= fin spacing, m
t	= fin thickness, m
T	= temperature, K
W	= enclosure width, m

Greek Symbols

α	= exponent in Archie's law, Eq. (9)
β	= coefficient of volume expansion, $1/K$
σ	= Stefan-Boltzman constant, W/m^2K^4
ε	= emissivity
ν	= kinematic viscosity, m^2/s

Subscripts

conv	= convective
fin	= related to fin

rad = radiation
total = radiation plus convective

References

- [1] Incropera, F. P., and De Witt, D. P., 1996, *Fundamentals of Heat and Mass Transfer*, 4th ed., J. Wiley & Sons, New York.
- [2] Starner, K. E., and McManus, H. N., 1963, "An Experimental Investigation of Free Convection Heat Transfer From Rectangular Fin Arrays," *ASME J. Heat Transfer*, **85**, pp. 273–278.
- [3] Welling, J. R., and Wooldridge, C. V., 1965, "Free Convection Heat Transfer Coefficients From Rectangular Fin Arrays," *ASME J. Heat Transfer*, **87**, pp. 439–444.
- [4] Harahap, F., and McManus, H. N., 1967, "Natural Convection Heat Transfer From Horizontal Rectangular Fin Arrays," *ASME J. Heat Transfer*, **89**, pp. 32–38.
- [5] Jones, C. D., and Smith, L. F., 1970, "Optimum Arrangement of Rectangular Fins on Horizontal Surfaces for Free Convection Heat Transfer," *ASME J. Heat Transfer*, **92**, pp. 6–10.
- [6] Donvan, R. C., and Roher, W. M., 1971, "Radiative and Convective Conducting Fins on a Plane Wall, Including Mutual Irradiation," *ASME J. Heat Transfer*, **93**, pp. 41–46.
- [7] Van de pol, D. W., and Tierney, J. K., 1974, "Free Convective Heat Transfer From Vertical Fin Arrays," *IEEE Trans. Parts Hybrids Packag.*, **10**(4), pp. 267–271.
- [8] Yuncu, H., and Anbar, G., 1998, "An Experimental Investigation on Performance of Rectangular Fins on a Horizontal Base in Free Convection Heat Transfer," *Heat Mass Transfer*, **33**, pp. 507–514.
- [9] Guvenc, A., and Yuncu, H., 2001, "An Experimental Investigation on Performance of Fins on a Horizontal Base in Free Convection Heat Transfer," *Heat Mass Transfer*, **37**(4–5), pp. 409–416.
- [10] Bar-Cohen, A., and Rohsenow, W. M., 1984, "Thermally Optimum Spacing of Vertical, Natural Convection Cooled, Parallel Plates," *J. Heat Transfer*, **116**, pp. 116–123.
- [11] Baskaya, S., Sivrioglu, M., and Ozek, M., 2000, "Parametric Study of Natural Convection Heat Transfer From Horizontal Rectangular Fin Arrays," *Int. J. Thermal Sci.*, **39**, pp. 797–805.
- [12] Haddad, O. M., and Bany-Youness, A., 2006, "Numerical Simulation of Natural Convection Flow Over Parabolic Bodies," *Int. J. Thermophys.*, **27**, pp. 1590–1608.
- [13] Dialameh, L., Yaghoubi, M., and Abouali, O., 2008, "Natural Convection From an Array of Horizontal Rectangular Thick Fins With Short Length," *Appl. Therm. Eng.*, **28**, pp. 2371–2379.
- [14] Edwards, J. A., and Chaddock, J. B., 1963, "An Experimental Investigation of the Radiation and Free Convection Heat Transfer From a Cylindrical Disk Extended Surface," *Trans. Am. Soc. Heat. Refrig. Air-Cond. Eng.*, **69**, pp. 313–322.
- [15] Chaddock, J. B., 1970, "Free Convection Heat Transfer From Vertical Fin Arrays," *ASHRAE J.*, **12**, pp. 53–60.
- [16] Sparrow, E. M., and Acharya, S., 1981, "A Natural Convection Fin With a Solution—Determined Nonmonotonically Varying Heat Transfer Coefficient," *ASME J. Heat Transfer*, **105**, pp. 218–225.
- [17] Saikhedkar, N. H., and Sukhatme, S. P., 1981, "Heat Transfer From Rectangular Cross-Sectioned Vertical Fin Arrays," *Proceedings of the Sixth National Heat and Mass Transfer Conference, HMT, 1981*, pp. 9–81.
- [18] Manzoor, M., Inham, D. B., and Heggs, P. J., 1983, "The One Dimensional Analysis of Fin Assembly Heat Transfer," *ASME J. Heat Transfer*, **105**, pp. 645–651.
- [19] Sparrow, E. M., and Vemuri, S. B., 1985, "Natural Convection–Radiation Heat Transfer From Highly Populated Pin Fin Arrays," *ASME J. Heat Transfer*, **107**, pp. 190–197.
- [20] Sparrow, E. M., and Vemuri, S. B., 1986, "Orientation Effects on Natural Convective/Radiation Pin-Fin Arrays," *Int. J. Heat Mass Transfer*, **29**, pp. 359–368.
- [21] Rao, V. D., Naidu, S. V., Rao, B. G., and Sharma, K. V., 2006, "Heat Transfer From a Horizontal Fin Array by Natural Convection and Radiation—A Conjugate Analysis," *Int. J. Heat Mass Transfer*, **49**, pp. 3379–3391.
- [22] Cha, D. J., and Cha, S. S., 1993, "Three-Dimensional Natural Convection Flow Around an Isothermal Cube," *Int. Commun. Heat Mass Transfer*, **20**, pp. 619–630.
- [23] Cha, D. J., and Cha, S. S., 1995, "Three-Dimensional Natural Convection Flows Around Two Interacting Isothermal Cubes," *Int. J. Heat Mass Transfer*, **38**, pp. 2343–2352.
- [24] Radziemska, E., and Lewandowski, W. M., 2008, "Experimental Verification of Natural Convective Heat Transfer Phenomenon From Isothermal Cuboids," *Exp. Thermal Fluid Sci.*, **32**, pp. 1034–1038.
- [25] Radziemska, E., and Lewandowski, W. M., 2003, "Natural Convective Heat Transfer From Isothermal Cuboids," *Int. J. Heat Mass Transfer*, **46**, pp. 2169–2178.
- [26] Lee, S., Yovanovich, M. M., and Jafarpur, K., 1991, "Effects of Geometry and Orientation on Laminar Natural Convection From Isothermal Bodies," *AIAA J. Thermophys. Heat Transfer*, **5**, pp. 208–216.
- [27] Cengel, Y., 2008, *Introduction to Thermodynamics and Heat Transfer*, 2nd ed., McGraw-Hill, New York.